1. A Math 105 Class at SWOCC is deciding on the next topic they will study. The choices are statistics (S), financial mathematics (F), and logic (L). On the day of the election, 20 students cast their ballots which are summarized by the following preference table.

Number of Votes	4	5	4	7
First Choice	L	F	L	S
Second Choice	S	S	F	F
Third Choice	F	L	S	L

(a) Using the plurality method, which choice wins the election?

(b) Is there a Condorcet Winner?

(c) Does this election violate Condorcet Criterion?

- A. (a) Choice L wins the election. (b) No. (c) Yes.
- B. (a) Choice L wins the election. (b) Yes. (c) No.
- C. (a) Choice S wins the election. (b) Yes. (c) Yes.
- D. (a) Choice L wins the election. (b) No. (c) No.
- E. (a) Choice S wins the election. (b) Yes. (c) No.
- F. (a) Choice S wins the election. (b) No. (c) No.
- G. (a) Choice L wins the election. (b) Yes. (c) Yes.
- H. (a) Choice S wins the election. (b) No. (c) Yes.

2. The board of directors of the S.P. Martini Wealth Management Company is electing a new CEO. Under consideration are candidates A, B, and C. The ballots were cast as follows:

B	C	C	C	C	C	B	A	B	B	B	C	B	B	B	B	B	B
C	A	B	A	A	A	A	C	C	A	C	B	A	C	C	A	A	A
A	B	A	B	B	B	C	B	A	C	A	A	C	A	A	C	C	C

How many people marked candidate C as their first choice?

A. 4

- B. 7
- C. 6
- D. 2
- E. 1
- F. 3
- G. 5
- H. 0

3. The Associated Student Government has put to a vote where their end-of-the-year banquet is to be held. The contenders are four following restaurants: Tokyo Bistro (T), Sharkbites (S), Captain's Choice (C), and the Pancake Mill (P).

T	S	C	T	T	S	P	P	P	S	C	P	T
S	T	S	P	P	T	C	S	T	C	S	C	C
P	C	T	C	S	P	S	T	C	P	T	S	S
C	P	P	S	C	C	T	C	S	T	P	T	P

How many people marked candidate P as their first choice?

- A. 1
- B. 6
- C. 2
- D. 3
- E. 4
- F. 7
- G. 0
- H. 5

4. Billy Bob is on the planning committee for the Oregon Moonshiners Association and has called for a vote on which city to hold their annual convention. This year the contenders are Coos Bay (C), Portland (P), and Eugene (E). The members of the committee cast their votes as follows:

Number of Votes	6	4	9	2
First Choice	P	P	C	C
Second Choice	C	E	P	E
Third Choice	E	C	E	P

(a) Using Instant Runoff Voting, which choice wins the election?

(b) Suppose every one in the first column changed their vote to C-E-P. Does this change the outcome of the election?

(c) Does your answer for part (b) cause this election to violate the Monotonicity Criterion?

A. (a) Choice C wins the election. (b) No. (c) Yes.

B. (a) Choice C wins the election. (b) Yes. (c) No.

C. (a) Choice P wins the election. (b) Yes. (c) Yes.

D. (a) Choice C wins the election. (b) Yes. (c) Yes.

E. (a) Choice P wins the election. (b) No. (c) No.

F. (a) Choice C wins the election. (b) No. (c) No.

G. (a) Choice P wins the election. (b) No. (c) Yes.

H. (a) Choice P wins the election. (b) Yes. (c) No.

5. A Math 105 Class at SWOCC is deciding on the next topic they will study. The choices are statistics (S), financial mathematics (F), and logic (L). On the day of the election, the students cast their ballots which are summarized by the following preference table.

Number of Votes	6	1	7	6	7	4
First Choice	S	S	F	F	L	L
Second Choice	F	L	S	L	S	F
Third Choice	L	F	L	S	F	S

Using the Borda-Count Method decide which choice, if any, wins the election.

- A. Candidate L won the election.
- B. Candidates S and F tied.
- C. Candidate F won the election.
- D. Candidates S and L tied.
- E. Candidates F and L tied.
- F. Candidate S won the election.
- G. All three Candidates tied.

6. A Math 105 Class at SWOCC is deciding on the next topic they will study. The choices are statistics (S), financial mathematics (F), and logic (L). On the day of the election, 20 students cast their ballots which are summarized by the following preference table.

Number of Votes	7	6	11	4
First Choice	S	S	L	L
Second Choice	F	L	S	F
Third Choice	L	F	F	S

(a) Using the Borda-Count Method, which choice wins the election?

(b) Is there a choice which has a majority of first-place votes?

(c) Does this election violate the majority criterion?

A. (a) Choice L wins the election. (b) No. (c) No.

B. (a) Choice S wins the election. (b) No. (c) Yes.

C. (a) Choice S wins the election. (b) Yes. (c) Yes.

D. (a) Choice L wins the election. (b) Yes. (c) Yes.

E. (a) Choice S wins the election. (b) Yes. (c) No.

F. (a) Choice S wins the election. (b) No. (c) No.

G. (a) Choice L wins the election. (b) No. (c) Yes.

H. (a) Choice L wins the election. (b) Yes. (c) No.

7. The Coos Bay chapter of Toastmasters International is deciding who they want to send to the state public speaking championship. The contenders are Wanda (W), Xavier (X), Yanni (Y), and Zelda (Z). The ballots were cast and tallied. The results are summarized by the preference table below.

Number of Votes	5	8	6
First Choice	W	X	Y
Second Choice	X	Z	Z
Third Choice	Y	Y	X
Fourth Choice	Z	W	W

Using the Borda-Count method, who, if anyone, won the election?

- A. Candidate X won the election.
- B. Candidate Y won the election.
- C. Candidate Z won the election.
- D. There was at least one tie for first place.
- E. Candidate W won the election.

8. The board of directors of the S.P. Martini Wealth Management Company is electing a new CEO. Under consideration are candidates A, B, and C. The ballots were cast and tallied. The results are summarized by the preference table below.

Number of Votes	13	15	14	16
First Choice	C	A	A	B
Second Choice	B	C	B	C
Third Choice	A	B	C	A

(a) Using the Pairwise Comparison Method, which choice wins the election?

(b) Suppose that the night before the election, a scandal exposes Candidate A's dark past, and in disgrace, candidate A drops out of the race. We do a recount of the ballots without A. Does this change the outcome of the election?

(c) Does your answer for part (b) cause this election to violate the Irrelevant Alternatives Criterion?

A. (a) Candidate C wins the election. (b) Yes. (c) No.

B. (a) Candidate B wins the election. (b) No. (c) Yes.

C. (a) Candidate B wins the election. (b) No. (c) No.

D. (a) Candidate C wins the election. (b) Yes. (c) Yes.

E. (a) Candidate C wins the election. (b) No. (c) Yes.

F. (a) Candidate C wins the election. (b) No. (c) No.

G. (a) Candidate B wins the election. (b) Yes. (c) Yes.

H. (a) Candidate B wins the election. (b) Yes. (c) No.

9. The board of directors of the S.P. Martini Wealth Management Company is electing a new CEO. Under consideration are candidates A, B, and C. The ballots were cast and tallied. The results are summarized by the preference table below.

Number of Votes	2	4	7	2	2	4
First Choice	A	A	B	B	C	C
Second Choice	B	C	A	C	A	B
Third Choice	C	B	C	A	B	A

Using the Pairwise Comparison Method, how many points did each candidate receive?

A. Candidate A: 1. Candidate B: 1.5. Candidate C: 0.5.

B. Candidate A: 1.5. Candidate B: 2.5. Candidate C: 1.

C. Candidate A: 2.5. Candidate B: 2. Candidate C: 1.5.

D. Candidate A: 2. Candidate B: 3. Candidate C: 2.

E. Candidate A: 3. Candidate B: 3. Candidate C: 3.

F. Candidate A: 3. Candidate B: 1. Candidate C: 1.

G. Candidate A: 1. Candidate B: 2. Candidate C: 0.

10. Billy Bob is on the planning committee for the Oregon Moonshiners Association and has called for a vote on which city to hold their annual convention. This year the contenders are Coos Bay (C), Portland (P), and Eugene (E). The members of the committee cast their votes as follows:

Number of Votes	6	4	7	3	4	7
First Choice	C	C	P	P	E	E
Second Choice	P	E	C	E	C	P
Third Choice	E	P	E	C	P	C

Using the Pairwise Comparison Method, how many points did each choice receive?

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- A. Choice C : 1. Choice P : 3.5. Choice E : 1.5.
- B. Choice C : 0.5. Choice P : 1. Choice E : 1.5.
- C. Choice C : 1. Choice P : 2. Choice E : 0.
- D. Choice C: 3. Choice P: 0.5. Choice E: 0.5.
- E. Choice C: 3.5. Choice P: 0. Choice E: 0.5.
- F. Choice C: 0. Choice P: 3. Choice E: 0.
- G. Choice C : 2.5. Choice P : 0. Choice E : 0.5.

## Answers

- 1. G.
- 2. C.
- 3. E.
- 4. F.
- 5. C.
- 6. C.
- 7. A.
- 8. C.
- 9. G.
- 10. C.